



## **AP<sup>®</sup> Physics C: Electricity and Magnetism 2007 Free-Response Questions**

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TABLE OF INFORMATION FOR 2006 and 2007

CONSTANTS AND CONVERSION FACTORS		UNITS		PREFIXES			
		Name	Symbol	Factor	Prefix	Symbol	
1 unified atomic mass unit,	$1 \text{ u} = 1.66 \times 10^{-27} \text{ kg}$ $= 931 \text{ MeV}/c^2$	meter	m	$10^9$	giga	G	
Proton mass,	$m_p = 1.67 \times 10^{-27} \text{ kg}$	kilogram	kg	$10^6$	mega	M	
Neutron mass,	$m_n = 1.67 \times 10^{-27} \text{ kg}$	second	s	$10^3$	kilo	k	
Electron mass,	$m_e = 9.11 \times 10^{-31} \text{ kg}$	ampere	A	$10^{-2}$	centi	c	
Electron charge magnitude,	$e = 1.60 \times 10^{-19} \text{ C}$	kelvin	K	$10^{-3}$	milli	m	
Avogadro's number,	$N_0 = 6.02 \times 10^{23} \text{ mol}^{-1}$	mole	mol	$10^{-6}$	micro	$\mu$	
Universal gas constant,	$R = 8.31 \text{ J}/(\text{mol}\cdot\text{K})$	hertz	Hz	$10^{-9}$	nano	n	
Boltzmann's constant,	$k_B = 1.38 \times 10^{-23} \text{ J}/\text{K}$	newton	N	$10^{-12}$	pico	p	
Speed of light,	$c = 3.00 \times 10^8 \text{ m}/\text{s}$	pascal	Pa	VALUES OF TRIGONOMETRIC FUNCTIONS FOR COMMON ANGLES			
Planck's constant,	$h = 6.63 \times 10^{-34} \text{ J}\cdot\text{s}$ $= 4.14 \times 10^{-15} \text{ eV}\cdot\text{s}$ $hc = 1.99 \times 10^{-25} \text{ J}\cdot\text{m}$ $= 1.24 \times 10^3 \text{ eV}\cdot\text{nm}$	joule	J				
Vacuum permittivity,	$\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N}\cdot\text{m}^2$	watt	W	$0^\circ$	0	1	0
Coulomb's law constant,	$k = 1/4\pi\epsilon_0 = 9.0 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$	coulomb	C	$30^\circ$	1/2	$\sqrt{3}/2$	$\sqrt{3}/3$
Vacuum permeability,	$\mu_0 = 4\pi \times 10^{-7} (\text{T}\cdot\text{m})/\text{A}$	volt	V	$37^\circ$	3/5	4/5	3/4
Magnetic constant,	$k' = \mu_0/4\pi = 10^{-7} (\text{T}\cdot\text{m})/\text{A}$	ohm	$\Omega$	$45^\circ$	$\sqrt{2}/2$	$\sqrt{2}/2$	1
Universal gravitational constant,	$G = 6.67 \times 10^{-11} \text{ m}^3/\text{kg}\cdot\text{s}^2$	henry	H	$53^\circ$	4/5	3/5	4/3
Acceleration due to gravity at Earth's surface,	$g = 9.8 \text{ m}/\text{s}^2$	farad	F	$60^\circ$	$\sqrt{3}/2$	1/2	$\sqrt{3}$
1 atmosphere pressure,	$1 \text{ atm} = 1.0 \times 10^5 \text{ N}/\text{m}^2$ $= 1.0 \times 10^5 \text{ Pa}$	tesla	T	$90^\circ$	1	0	$\infty$
1 electron volt,	$1 \text{ eV} = 1.60 \times 10^{-19} \text{ J}$	degree Celsius	$^\circ\text{C}$				
		electron-volt	eV				

The following conventions are used in this examination.

- I. Unless otherwise stated, the frame of reference of any problem is assumed to be inertial.
- II. The direction of any electric current is the direction of flow of positive charge (conventional current).
- III. For any isolated electric charge, the electric potential is defined as zero at an infinite distance from the charge.



**ADVANCED PLACEMENT PHYSICS C EQUATIONS FOR 2006 and 2007**

**GEOMETRY AND TRIGONOMETRY**

Rectangle

$$A = bh$$

Triangle

$$A = \frac{1}{2}bh$$

Circle

$$A = \pi r^2$$

$$C = 2\pi r$$

Parallelepiped

$$V = \ell wh$$

Cylinder

$$V = \pi r^2 \ell$$

$$S = 2\pi r \ell + 2\pi r^2$$

Sphere

$$V = \frac{4}{3}\pi r^3$$

$$S = 4\pi r^2$$

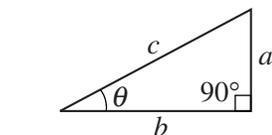
Right Triangle

$$a^2 + b^2 = c^2$$

$$\sin \theta = \frac{a}{c}$$

$$\cos \theta = \frac{b}{c}$$

$$\tan \theta = \frac{a}{b}$$



$A$  = area  
 $C$  = circumference  
 $V$  = volume  
 $S$  = surface area  
 $b$  = base  
 $h$  = height  
 $\ell$  = length  
 $w$  = width  
 $r$  = radius

**CALCULUS**

$$\frac{df}{dx} = \frac{df}{du} \frac{du}{dx}$$

$$\frac{d}{dx}(x^n) = nx^{n-1}$$

$$\frac{d}{dx}(e^x) = e^x$$

$$\frac{d}{dx}(\ln x) = \frac{1}{x}$$

$$\frac{d}{dx}(\sin x) = \cos x$$

$$\frac{d}{dx}(\cos x) = -\sin x$$

$$\int x^n dx = \frac{1}{n+1} x^{n+1}, n \neq -1$$

$$\int e^x dx = e^x$$

$$\int \frac{dx}{x} = \ln|x|$$

$$\int \cos x dx = \sin x$$

$$\int \sin x dx = -\cos x$$

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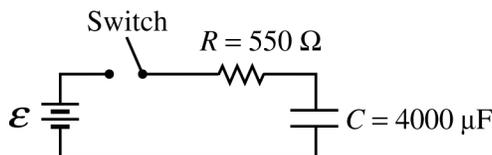
**PHYSICS C: ELECTRICITY AND MAGNETISM**

**SECTION II**

**Time—45 minutes**

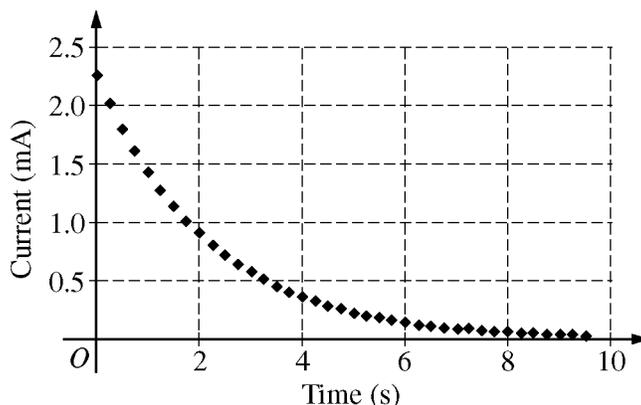
**3 Questions**

**Directions:** Answer all three questions. The suggested time is about 15 minutes for answering each of the questions, which are worth 15 points each. The parts within a question may not have equal weight. Show all your work in the pink booklet in the spaces provided after each part, NOT in this green insert.



E&M 1.

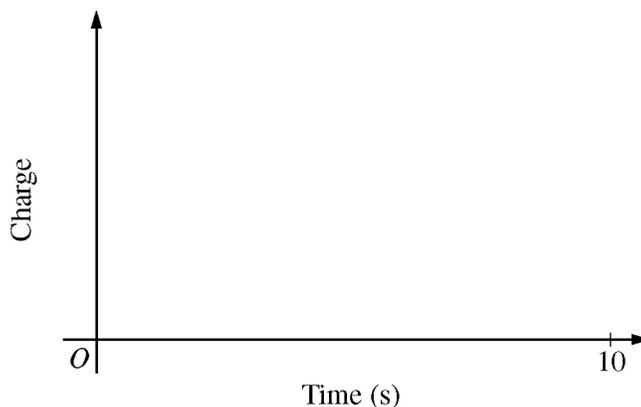
A student sets up the circuit above in the lab. The values of the resistance and capacitance are as shown, but the constant voltage  $\mathcal{E}$  delivered by the ideal battery is unknown. At time  $t = 0$ , the capacitor is uncharged and the student closes the switch. The current as a function of time is measured using a computer system, and the following graph is obtained.



- Using the data above, calculate the battery voltage  $\mathcal{E}$ .
- Calculate the voltage across the capacitor at time  $t = 4.0$  s.
- Calculate the charge on the capacitor at  $t = 4.0$  s.

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(d) On the axes below, sketch a graph of the charge on the capacitor as a function of time.

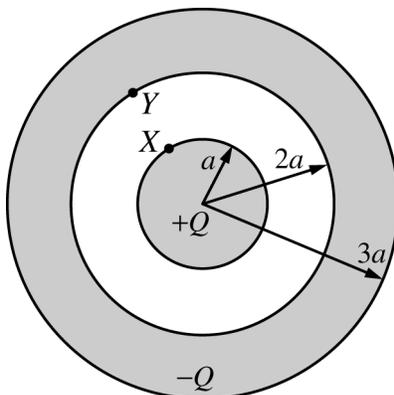


(e) Calculate the power being dissipated as heat in the resistor at  $t = 4.0$  s.

(f) The capacitor is now discharged, its dielectric of constant  $\kappa = 1$  is replaced by a dielectric of constant  $\kappa = 3$ , and the procedure is repeated. Is the amount of charge on one plate of the capacitor at  $t = 4.0$  s now greater than, less than, or the same as before? Justify your answer.

\_\_\_\_\_ Greater than    \_\_\_\_\_ Less than    \_\_\_\_\_ The same

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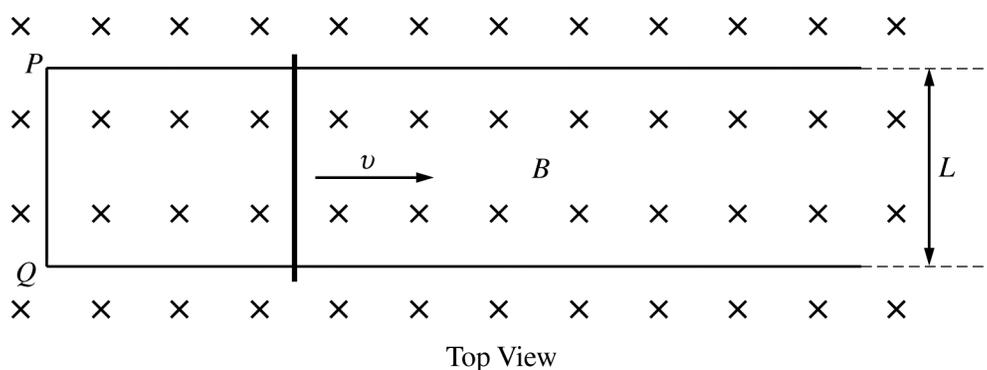


E&M 2.

In the figure above, a nonconducting solid sphere of radius  $a$  with charge  $+Q$  uniformly distributed throughout its volume is concentric with a nonconducting spherical shell of inner radius  $2a$  and outer radius  $3a$  that has a charge  $-Q$  uniformly distributed throughout its volume. Express all answers in terms of the given quantities and fundamental constants.

- (a) Using Gauss's law, derive expressions for the magnitude of the electric field as a function of radius  $r$  in the following regions.
- Within the solid sphere ( $r < a$ )
  - Between the solid sphere and the spherical shell ( $a < r < 2a$ )
  - Within the spherical shell ( $2a < r < 3a$ )
  - Outside the spherical shell ( $r > 3a$ )
- (b) What is the electric potential at the outer surface of the spherical shell ( $r = 3a$ )? Explain your reasoning.
- (c) Derive an expression for the electric potential difference  $V_X - V_Y$  between points  $X$  and  $Y$  shown in the figure.

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E&M 3.

In the diagram above, a nichrome wire of resistance per unit length  $\lambda$  is bent at points  $P$  and  $Q$  to form horizontal conducting rails that are a distance  $L$  apart. The wire is placed within a uniform magnetic field of magnitude  $B$  pointing into the page. A conducting rod of negligible resistance, which was aligned with end  $PQ$  at time  $t = 0$ , slides to the right with constant speed  $v$  and negligible friction. Express all algebraic answers in terms of the given quantities and fundamental constants.

- (a) Indicate the direction of the current induced in the circuit.

\_\_\_\_\_ Clockwise      \_\_\_\_\_ Counterclockwise

Justify your answer.

- (b) Derive an expression for the magnitude of the induced current as a function of time  $t$ .  
 (c) Derive an expression for the magnitude of the magnetic force on the rod as a function of time.  
 (d) On the axes below, sketch a graph of the external force  $F_{ext}$  as a function of time that must be applied to the rod to keep it moving at constant speed while in the field. Label the values of any intercepts.



- (e) The force pulling the rod is now removed. Indicate whether the speed of the rod increases, decreases, or remains the same.

\_\_\_\_\_ Increases      \_\_\_\_\_ Decreases      \_\_\_\_\_ Remains the same

Justify your answer.

**END OF EXAM**